



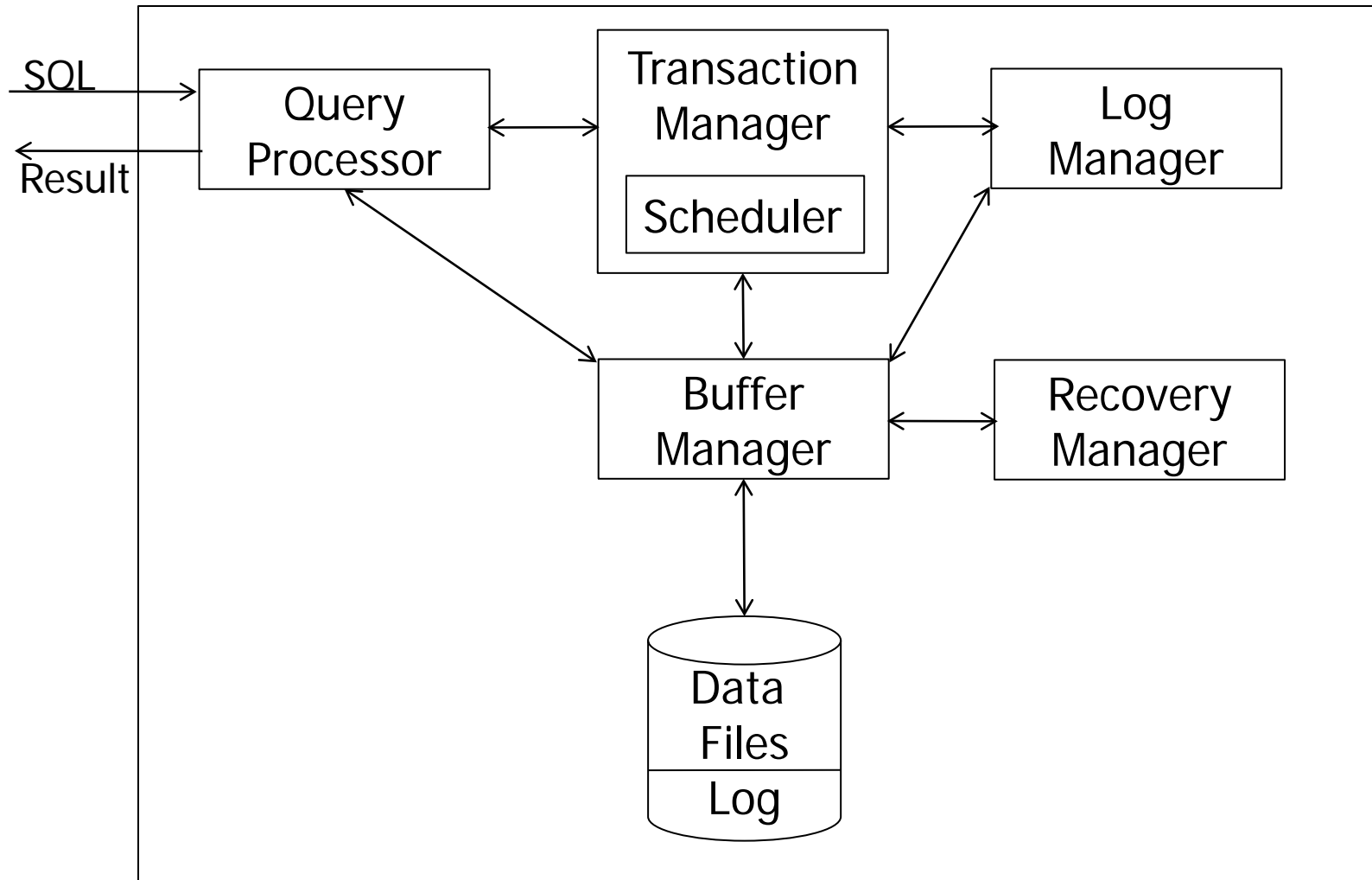
CSCD43: Database Systems Technology

Lecture 12

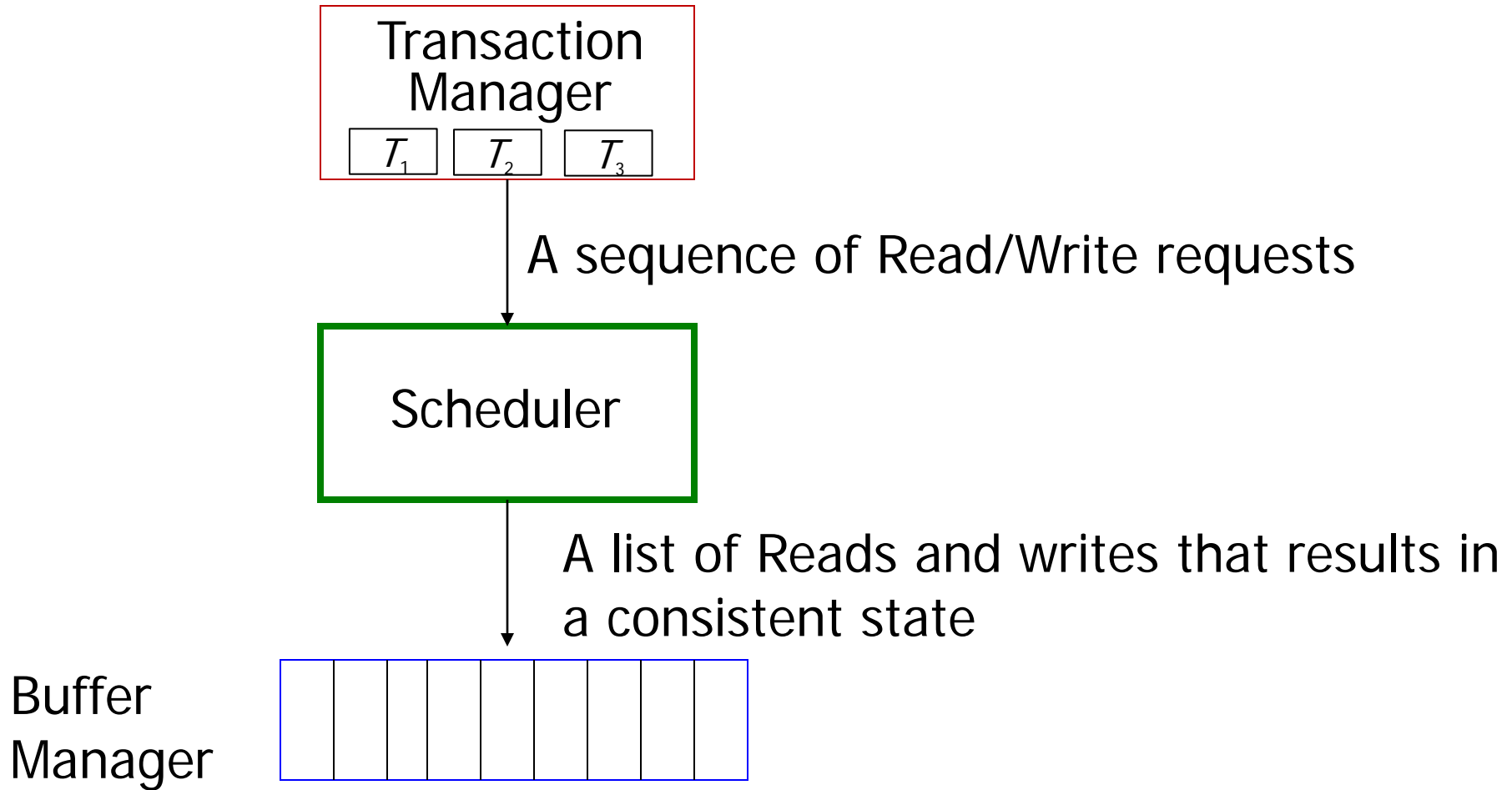
Wael Aboulsaadat

Acknowledgment: these slides are based on Prof. Garcia-Molina & Prof. Ullman slides accompanying the course's textbook.

DBMS Architecture



Component for Concurrency Control





Transactions

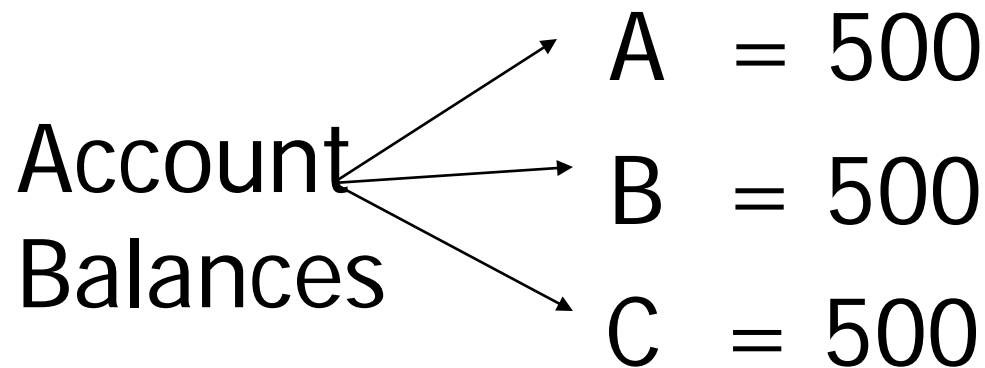
- Historical note:
 - Turing Award for Transaction concept
 - Jim Gray (1998)
- Interesting reading:

Transaction Concept: Virtues and Limitations by Jim Gray

<http://www.hpl.hp.com/techreports/tandem/TR-81.3.pdf>

Issues with Transactions: Example

Bank database: 3 Accounts



Property: $A + B + C = 1500$

Money does not leave the system

Issues with Transactions: Example

Transaction T1: Transfer 100 from A to B

$A = 500, B = 500, C = 500$ →

Read (A, t)

$t = t - 100$

Write (A, t)

Read (B, t)

$t = t + 100$

Write (B, t)

$A = 400, B = 600, C = 500$ →

Issues with Transactions: Example

Transaction T2: Transfer 100 from A to C

$A = 500, B = 500, C = 500$ →

Read (A, s)

$s = s - 100$

Write (A, s)

Read (C, s)

$s = s + 100$

Write (C, s)

$A = 400, B = 500, C = 600$ →



Transaction T1

Transaction T2

A

B

C

Read (A, t)

$t = t - 100$

Write (A, t)

Read (B, t)

$t = t + 100$

Write (B, t)

Read (A, s)

$s = s - 100$

Write (A, s)

Read (C, s)

$s = s + 100$

Write (C, s)

500

500

500

400

500

500

400

600

500

300

600

500

300

600

600

$300 + 600 + 600 = 1500$



Transaction T1

Transaction T2

A

B

C

Read (A, t)

$t = t - 100$

Write (A, t)

Read (A, s)

$s = s - 100$

Write (A, s)

Read (B, t)

$t = t + 100$

Write (B, t)

Read (C, s)

$s = s + 100$

Write (C, s)

500

500

500

400

500

500

300

500

500

300

600

500

300

600

600

$300 + 600 + 600 = 1500$



Transaction T1

Transaction T2

A

B

C

Read (A, t)

$t = t - 100$

Read (A, s)

$s = s - 100$

Write (A, s)

Write (A, t)

Read (B, t)

$t = t + 100$

Write (B, t)

Read (C, s)

$s = s + 100$

Write (C, s)

500

500

500

400

500

500

400

500

500

400

600

500

400

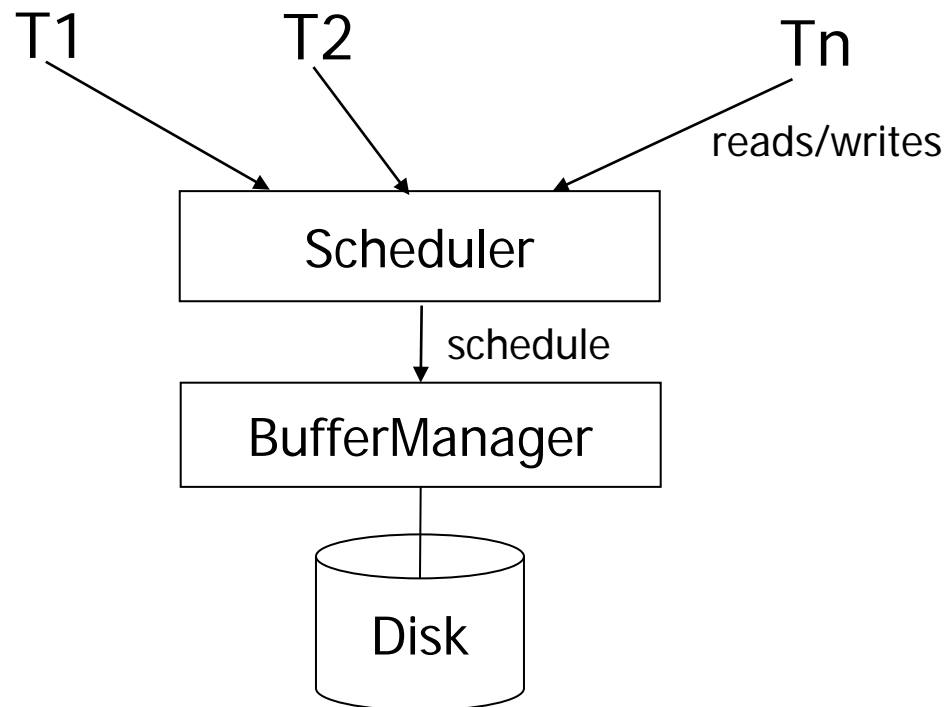
600

600

$400 + 600 + 600 = 1600$

Terminology

- Schedule:
 - The exact sequence of (relevant) actions of one or more transactions





Problems

- Which schedules are “correct”?
 - Mathematical characterization
- How to build a system that allows only “correct” schedules?
 - Efficient procedure to enforce correctness



Serial Schedule

		A	B	C
	Read (A, t)	500	500	500
	t = t - 100			
T1	Write (A, t)			
	Read (B, t)			
	t = t + 100			
	Write (B, t)	400	600	500
	Read (A, s)			
	s = s - 100			
	Write (A, s)			
T2	Read (C, s)			
	s = s + 100			
	Write (C, s)	300	600	600

300 + 600 + 600 = 1500

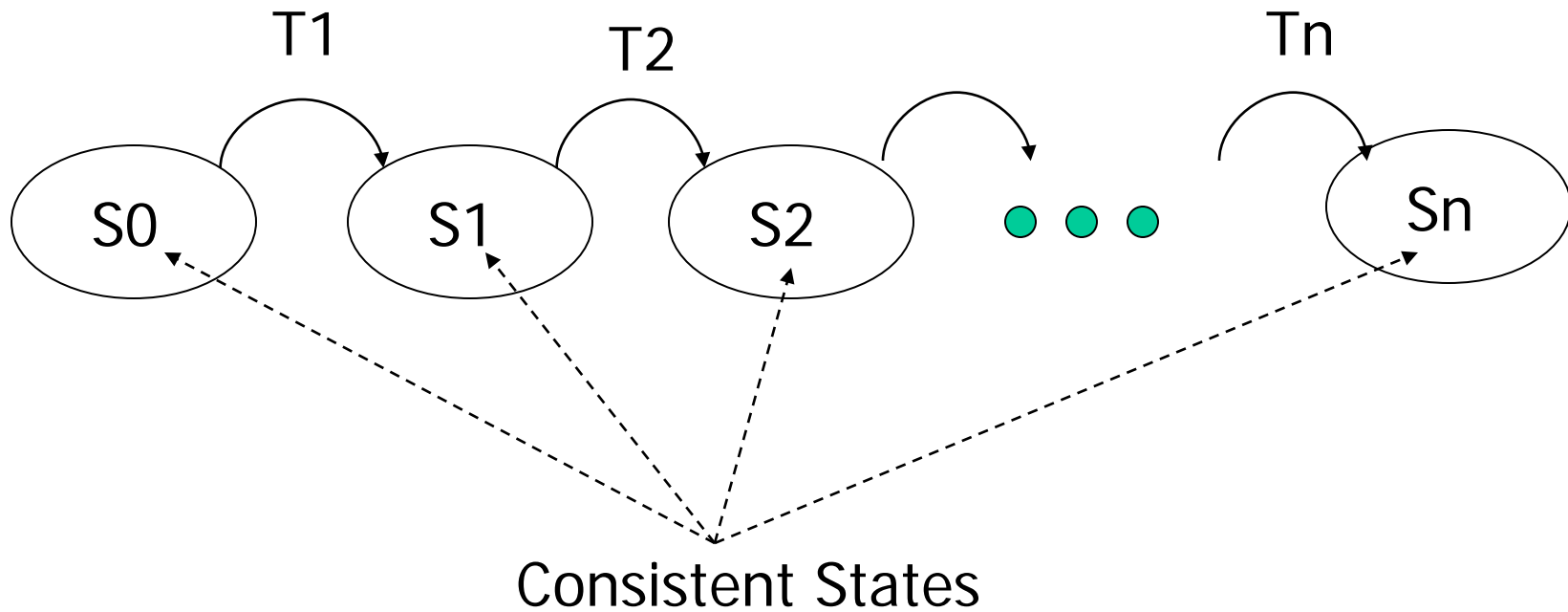


Serial Schedule

		A	B	C
T2	Read (A, s)	500	500	500
	$s = s - 100$			
	Write (A, s)			
	Read (C, s)			
	$s = s + 100$			
T1	Write (C, s)	400	500	600
	Read (A, t)			
	$t = t - 100$			
	Write (A, t)			
	Read (B, t)			
T1	$t = t + 100$			
	Write (B, t)			
		300	600	600

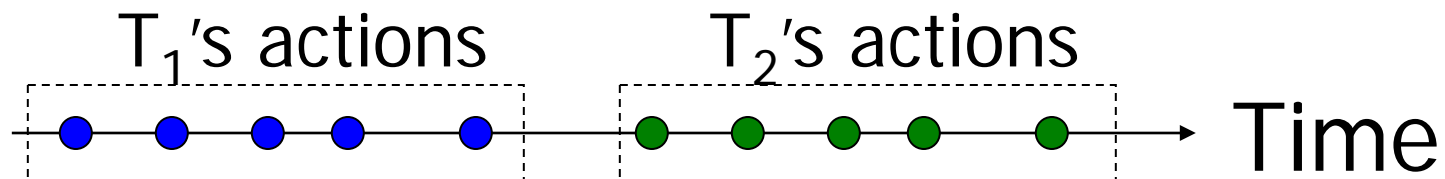
$300 + 600 + 600 = 1500$

Serial Schedule



Serial Schedule

- If any action of transaction T_1 precedes any action of T_2 , then all action of T_1 precede all action of T_2
- The correctness principle tells us that every serial schedule will preserve consistency of the database state



- What's the problem with a Serial Schedule?



Serializability

- A schedule is called *serializable* if its final effect is the same as that of a *serial schedule*
- Serializability \rightarrow schedule is fine and does not result in inconsistent database
 - Since serial schedules are fine
- Non-serializable schedules are unlikely to result in consistent databases
- Scheduler ensures serializability

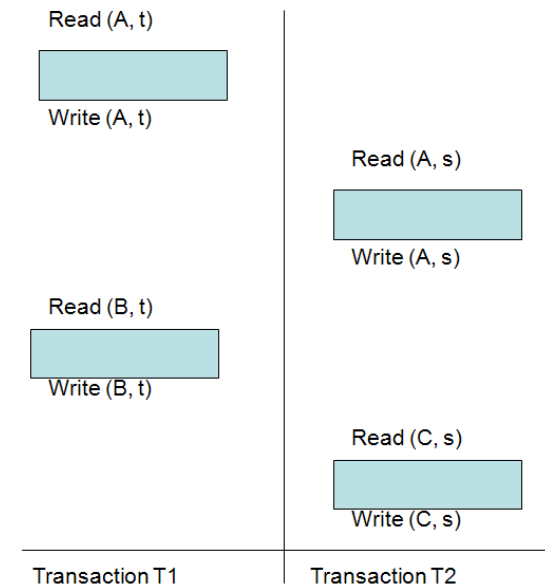


Serializability

- Not possible to look at all $n!$ serial schedules to check if the effect is the same
 - Instead we ensure serializability by allowing or not allowing certain schedules

Conflict Serializability

- Weaker notion of serializability
- Depends only on reads and writes
- Which steps can be interleaved and which cannot





Conflict Serializability

- Recall from OS course:
 - Multitasking
 - context switch



T1	T2	T1	T2
read(A) A = A - 50 write(A)	read(A) tmp = A*0.1 A = A - tmp write(A)	read(A) A = A - 50 write(A)	read(A) tmp = A*0.1 A = A - tmp
read(B) B=B+50 write(B)	read(B) B = B+ tmp write(B)	read(B) B=B+50 write(B)	write(A) read(B) B = B+ tmp write(B)

Effect:	<u>Before</u>	<u>After</u>		Effect:	<u>Before</u>	<u>After</u>
	A	100		A	100	45
	B	50	==	B	50	105



T1	T2	T1	T2
read(A) A = A - 50 write(A)	read(A) tmp = A * 0.1 A = A - tmp write(A)	read(A) A = A - 50 write(A)	read(A) tmp = A * 0.1 A = A - tmp write(A)
read(B) B = B + 50 write(B)	read(B) B = B + tmp write(B)	read(B) B = B + 50	read(B)
		write(B)	B = B + tmp write(B)

Effect:	<u>Before</u>	<u>After</u>		Effect:	<u>Before</u>	<u>After</u>
A	100	45	! ==	A	100	45
B	50	105		B	50	55



T1	T2	T1	T2
read(A) A = A - 50 write(A)	read(A) tmp = A * 0.1 A = A - tmp write(A)	read(A) A = A - 50 write(A)	read(A) tmp = A * 0.1 A = A - tmp
read(B) B = B + 50 write(B)	read(B) B = B + tmp write(B)	read(B) B = B + 50 write(B)	write(A)

Effect:	<u>Before</u>	<u>After</u>		Effect:	<u>Before</u>	<u>After</u>
A	100	45	==	A	100	45
B	50	105		B	50	105



T1		T2		T1		T2	
read(A)				read(A)			
A = A - 50				A = A - 50			
write(A)				write(A)			
		read(A)		read(B)		read(A)	
		tmp = A * 0.1		B = B + 50		tmp = A * 0.1	
		A = A - tmp		write(B)		A = A - tmp	
		write(A)				write(A)	
read(B)							
B = B + 50							
write(B)							
		read(B)				read(B)	
		B = B + tmp				B = B + tmp	
		write(B)				write(B)	

Effect:	<u>Before</u>	<u>After</u>		Effect:	<u>Before</u>	<u>After</u>
A	100	45	==	A	100	45
B	50	105		B	50	105

Simpler Notation

$r_T(X)$ Transaction T reads X

$w_T(X)$ Transaction T writes X

What is X in $r(X)$?

- X could be any component of a database:
 - Attribute of a tuple
 - Tuple
 - Block in which a tuple resides
 - A relation
 - ...



Non-Conflicting Steps

- Two Reads
 - E.g., $r_i(X); r_j(Y)$
- Read and write of different database element
 - E.g., $r_i(X); w_j(Y)$
- Two writes of different database elements
 - E.g., $w_i(X); w_j(Y)$



Conflicting Steps

- Two actions of the same transaction
 - E.g., $r_i(X); w_i(Y)$
- Two writes of the same database element
 - E.g., $w_i(X); w_j(X)$
- A read and a write of the same database element
 - E.g., $r_i(X); w_j(X)$



Conflict Serializability

- Conflict-equivalent schedules:
 - If S can be transformed into S' through a series of swaps, S and S' are called *conflict-equivalent*
 - *conflict-equivalent guarantees same final effect on the database*
- A schedule S is conflict-serializable if it is conflict-equivalent to a serial schedule



Conflict-Serializability

- Commercial systems generally support *conflict-serializability*
 - Stronger notion than serializability
- Turn a given schedule to a serial one by make as many nonconflicting swaps as we wish



Testing for conflict-serializability

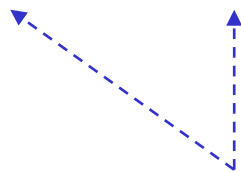
- Given a schedule, determine if it is conflict-serializable
- Construct a *precedence-graph* over the transactions
 - A directed edge from T1 and T2, if they have conflicting instructions, and T1's conflicting instruction comes first
- If there is a cycle in the graph, not conflict-serializable
 - Can be checked in at most $O(n+e)$ time, where n is the number of vertices, and e is the number of edges
- If there is none, conflict-serializable

Precedence Graph

- Precedence graph for schedule S:

- Nodes: Transactions in S
- Edges: $T_i \rightarrow T_j$ whenever

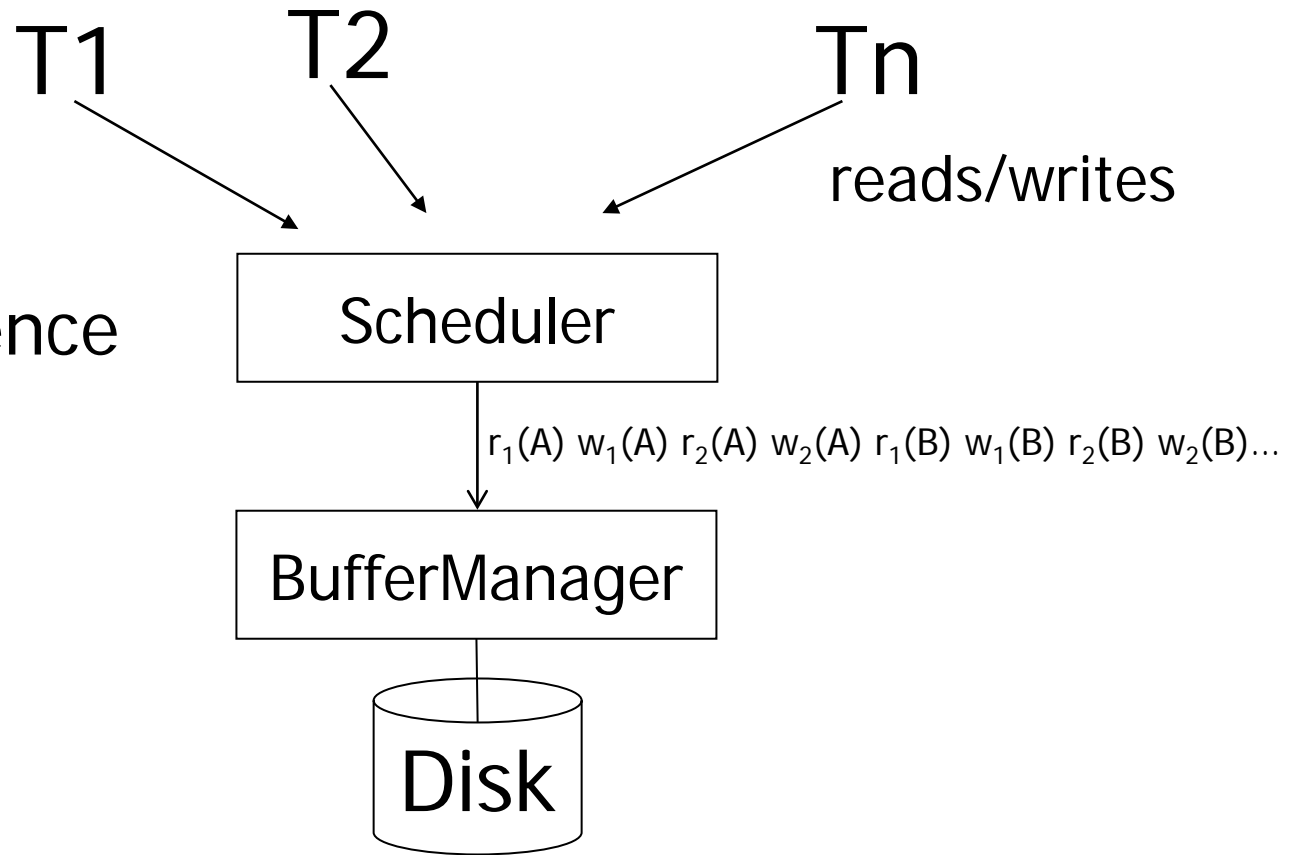
- S: ... $r_i(X)$... $w_i(X)$...
- S: ... $w_i(X)$... $w_j(X)$...
- S: ... $r_i(X)$... $w_j(X)$...



Note: not necessarily consecutive

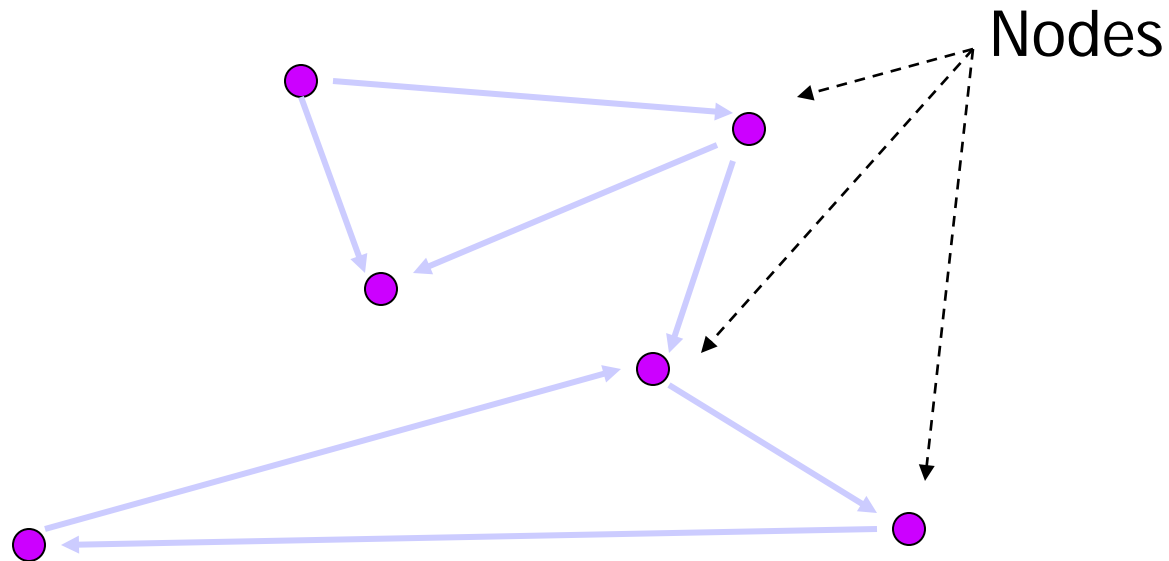
Enforcing Serializability

Strategy:
Prevent precedence
graph cycles



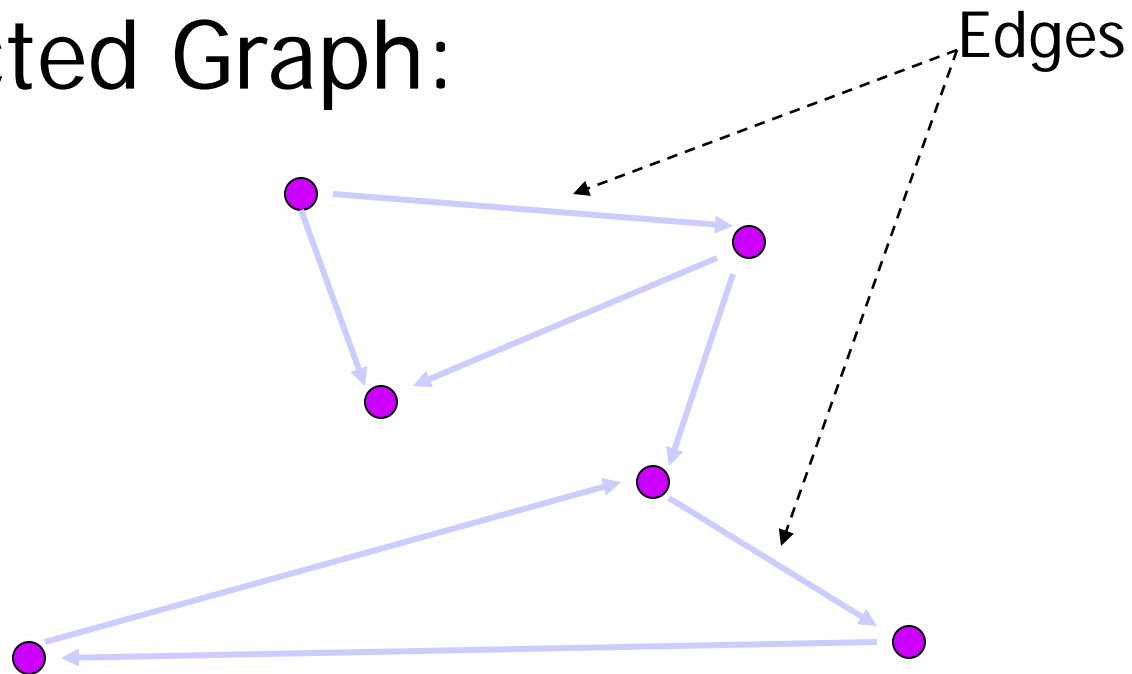
Graph Theory 101

Directed Graph:



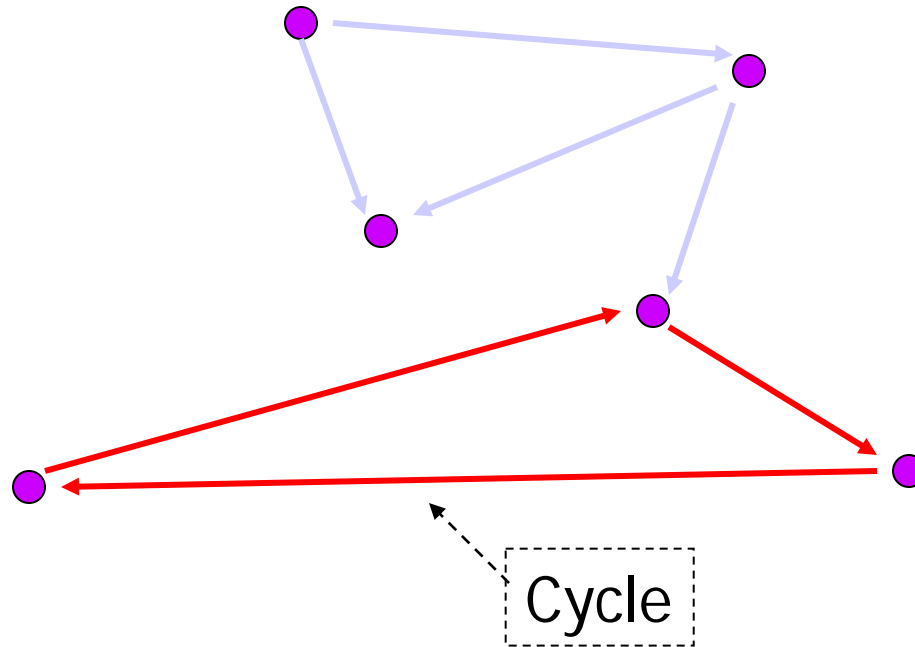
Graph Theory 101

Directed Graph:



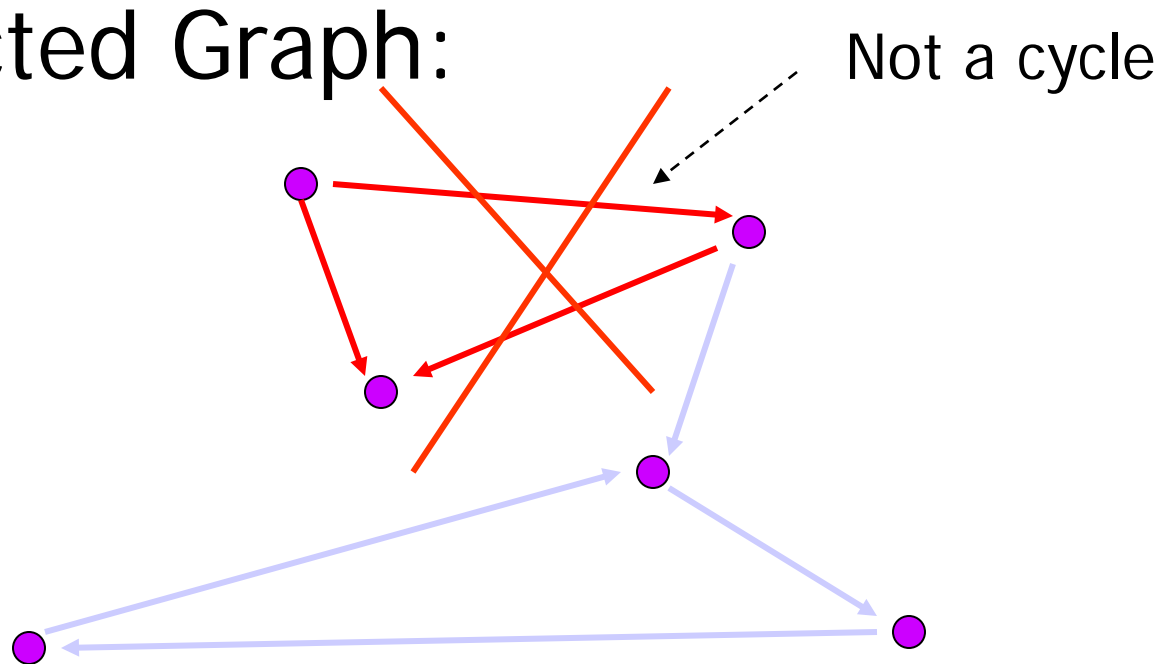
Graph Theory 101

Directed Graph:



Graph Theory 101

Directed Graph:



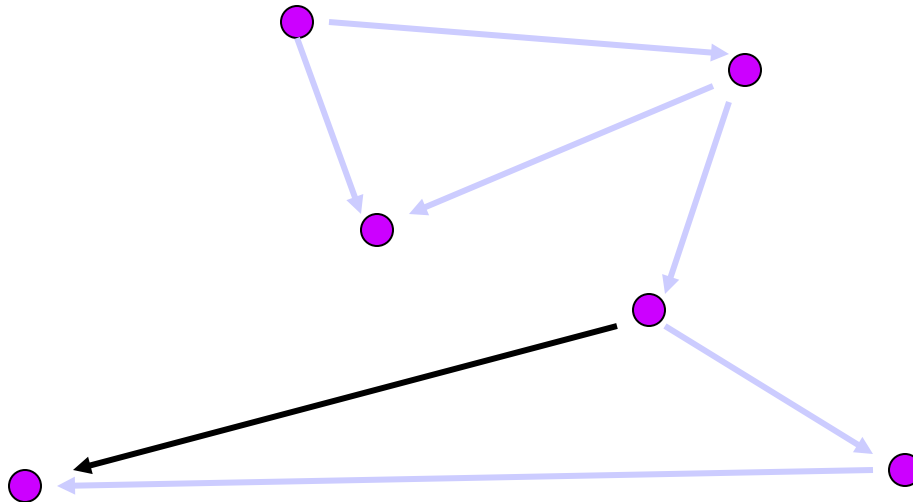


Graph Theory 101

Acyclic Graph: A graph with no cycles

Graph Theory 101

Acyclic Graph:





Precedence Graph - Example

- $T_i \rightarrow T_j$ whenever:
 - There is an action of T_i that occurs before a conflicting action of T_j .

$r_i(X); w_i(Y)$
$w_i(X); w_j(X)$
$r_i(X); w_j(X)$



Precedence Graph – Example 1

- $T_i \rightarrow T_j$ whenever:
 - There is an action of T_i that occurs before a conflicting action of T_j .

$S_1: r_2(A); r_1(B); w_2(A); r_3(A); w_1(B); w_3(A); r_2(B); w_2(B);$

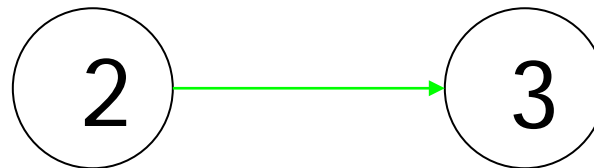
$r_i(X); w_i(Y)$
$w_i(X); w_j(X)$
$r_i(X); w_j(X)$



Precedence Graph – Example 1

- $T_i \rightarrow T_j$ whenever:
 - There is an action of T_i that occurs before a conflicting action of T_j .

$S_1: \underbrace{r_2(A); r_1(B); w_2(A); r_3(A); w_1(B); w_3(A)}; r_2(B); w_2(B);$



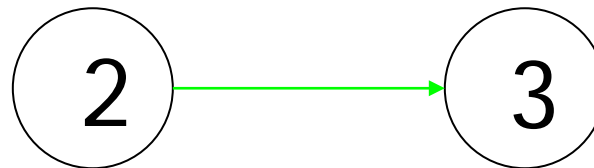
$r_i(X); w_i(Y)$
$w_i(X); w_j(X)$
$r_i(X); w_j(X)$



Precedence Graph – Example 1

- $T_i \rightarrow T_j$ whenever:
 - There is an action of T_i that occurs before a conflicting action of T_j .

$S_1: r_2(A); r_1(B); w_2(A); r_3(A); w_1(B); w_3(A); r_2(B); w_2(B);$



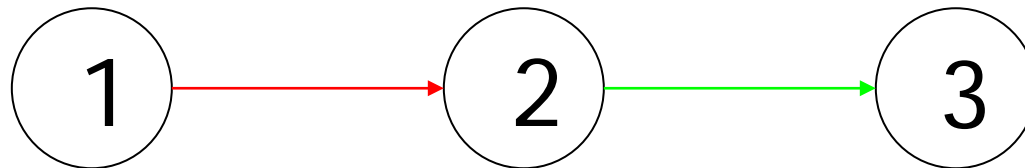
$r_i(X); w_i(Y)$
$w_i(X); w_j(X)$
$r_i(X); w_j(X)$



Precedence Graph – Example 1

- $T_i \rightarrow T_j$ whenever:
 - There is an action of T_i that occurs before a conflicting action of T_j .

$S_1: r_2(A); r_1(B); w_2(A); r_3(A); w_1(B); w_3(A); r_2(B); w_2(B);$



$r_i(X); w_i(Y)$
$w_i(X); w_j(X)$
$r_i(X); w_j(X)$



Precedence Graph – Example 2

- $T_i \rightarrow T_j$ whenever:
 - There is an action of T_i that occurs before a conflicting action of T_j .

$S_2: r_2(A); r_1(B); w_2(A); r_2(B); r_3(A); w_1(B); w_3(A); w_2(B);$

$r_i(X); w_i(Y)$
$w_i(X); w_j(X)$
$r_i(X); w_j(X)$

Precedence Graph – Example 2

- $T_i \rightarrow T_j$ whenever:
 - There is an action of T_i that occurs before a conflicting action of T_j .

S_2 : $r_2(A)$; $r_1(B)$; $w_2(A)$; $r_2(B)$; $r_3(A)$; $w_1(B)$; $w_3(A)$; $w_2(B)$;

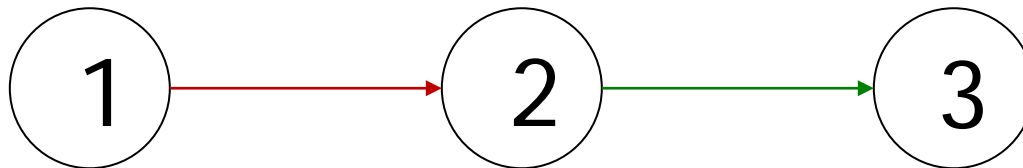


$r_i(X)$; $w_i(Y)$
$w_i(X)$; $w_j(X)$
$r_i(X)$; $w_j(X)$

Precedence Graph – Example 2

- $T_i \rightarrow T_j$ whenever:
 - There is an action of T_i that occurs before a conflicting action of T_j .

S_2 : $r_2(A)$; $r_1(B)$; $w_2(A)$; $r_2(B)$; $r_3(A)$; $w_1(B)$; $w_3(A)$; $w_2(B)$;

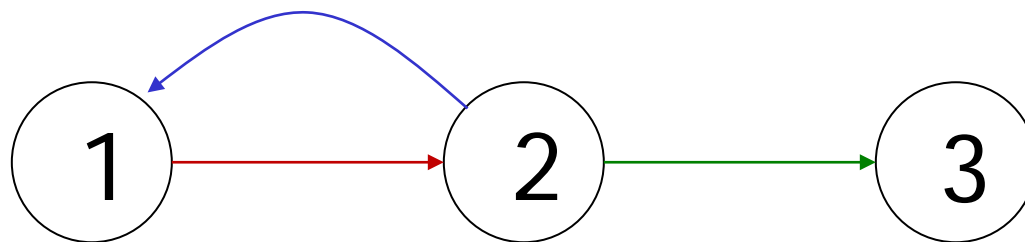


$r_i(X)$; $w_i(Y)$
$w_i(X)$; $w_j(X)$
$r_i(X)$; $w_j(X)$

Precedence Graph – Example 2

- $T_i \rightarrow T_j$ whenever:
 - There is an action of T_i that occurs before a conflicting action of T_j .

S_2 : $r_2(A)$; $r_1(B)$; $w_2(A)$; $r_2(B)$; $r_3(A)$; $w_1(B)$; $w_3(A)$; $w_2(B)$;

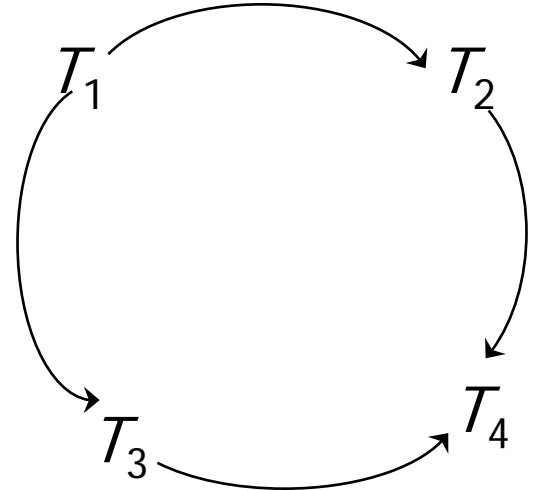


$r_i(X)$	$w_i(Y)$
$w_i(X)$	$w_j(X)$
$r_i(X)$	$w_j(X)$



Precedence Graph – Example 3

T_1	T_2	T_3	T_4	T_5
read(Y) read(Z)	read(X)			read(V) read(W) read(W)
	read(Y) write(Y)	write(Z)		
read(U)			read(Y) write(Y) read(Z) write(Z)	
read(U) write(U)				



$r_i(X); w_i(Y)$
 $w_i(X); w_j(X)$
 $r_i(X); w_j(X)$

$r_2(X); r_1(Y); r_1(Z); r_5(V); r_5(W); r_5(W); r_2(Y); w_2(Y); w_3(Z); r_1(U); r_4(Y); w_4(Y); r_4(Z); w_4(Z); r_1(U); w_1(U)$



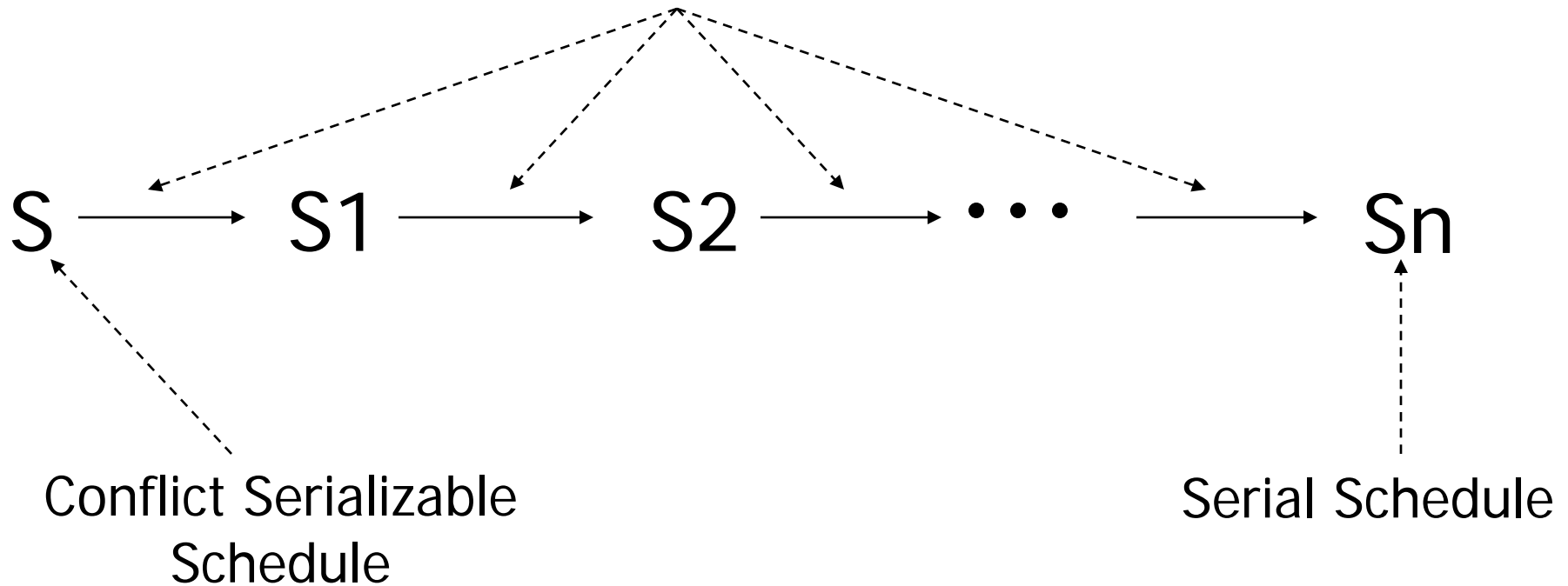
Conflict-serializable

- Two schedules are *conflict-equivalent* if they can be turned one into the other by a sequence of nonconflicting swaps of adjacent actions
- A schedule is *conflict-serializable* if it is conflict-equivalent to a serial schedule

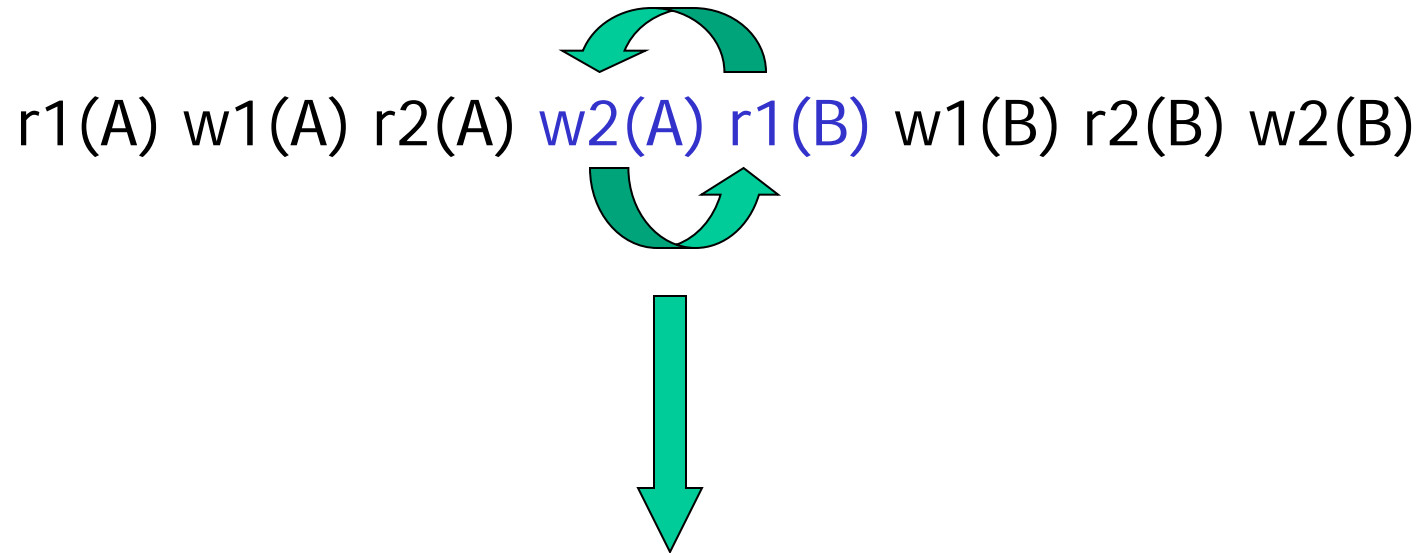


Conflict Serializable Schedule

Transformations: swap **non-conflicting** actions



Transformation





Transformation: Example

$r_i(X); r_i(Y)$
 $r_i(X); r_i(Y)$
 $w_i(X); w_j(Y)$

$r_1(A); w_1(A); r_2(A); w_2(A); r_1(B); w_1(B); r_2(B); w_2(B)$



Transformation: Example

$r_i(X); r_i(Y)$
 $r_i(X); r_i(Y)$
 $w_i(X); w_j(Y)$

$r_1(A); w_1(A); r_2(A); w_2(A); r_1(B); w_1(B); r_2(B); w_2(B)$



Transformation: Example

$r_i(X); r_i(Y)$
 $r_i(X); r_i(Y)$
 $w_i(X); w_j(Y)$

$r_1(A); w_1(A); r_2(A); w_2(A); r_1(B); w_1(B); r_2(B); w_2(B)$

$r_1(A); w_1(A); r_2(A); r_1(B); w_2(A); w_1(B); r_2(B); w_2(B)$



Transformation: Example

$r_i(X); r_i(Y)$
 $r_i(X); r_i(Y)$
 $w_i(X); w_j(Y)$

$r_1(A); w_1(A); r_2(A); w_2(A); r_1(B); w_1(B); r_2(B); w_2(B)$

$r_1(A); w_1(A); r_2(A); r_1(B); w_2(A); w_1(B); r_2(B); w_2(B)$

Transformation: Example

$r_i(X); r_i(Y)$
 $r_i(X); r_i(Y)$
 $w_i(X); w_j(Y)$

$r_1(A); w_1(A); r_2(A); w_2(A); r_1(B); w_1(B); r_2(B); w_2(B)$

$r_1(A); w_1(A); r_2(A); r_1(B); w_2(A); w_1(B); r_2(B); w_2(B)$

$r_1(A); w_1(A); r_1(B); r_2(A); w_2(A); w_1(B); r_2(B); w_2(B)$

Transformation: Example

$r_i(X); r_i(Y)$
 $r_i(X); r_i(Y)$
 $w_i(X); w_j(Y)$

$r_1(A); w_1(A); r_2(A); w_2(A); r_1(B); w_1(B); r_2(B); w_2(B)$

$r_1(A); w_1(A); r_2(A); r_1(B); w_2(A); w_1(B); r_2(B); w_2(B)$

$r_1(A); w_1(A); r_1(B); r_2(A); w_2(A); w_1(B); r_2(B); w_2(B)$

Transformation: Example

$r_i(X); r_i(Y)$ $r_i(X); r_i(Y)$ $w_i(X); w_j(Y)$
--

$r_1(A); w_1(A); r_2(A); w_2(A); r_1(B); w_1(B); r_2(B); w_2(B)$

$r_1(A); w_1(A); r_2(A); r_1(B); w_2(A); w_1(B); r_2(B); w_2(B)$

$r_1(A); w_1(A); r_1(B); r_2(A); w_2(A); w_1(B); r_2(B); w_2(B)$

$r_1(A); w_1(A); r_1(B); r_2(A); w_1(B); w_2(A); r_2(B); w_2(B)$



Transformation: Example

$r_i(X); r_i(Y)$
 $r_i(X); r_i(Y)$
 $w_i(X); w_j(Y)$

$r_1(A); w_1(A); r_2(A); w_2(A); r_1(B); w_1(B); r_2(B); w_2(B)$

$r_1(A); w_1(A); r_2(A); r_1(B); w_2(A); w_1(B); r_2(B); w_2(B)$

$r_1(A); w_1(A); r_1(B); r_2(A); w_2(A); w_1(B); r_2(B); w_2(B)$

$r_1(A); w_1(A); r_1(B); r_2(A); w_1(B); w_2(A); r_2(B); w_2(B)$



Transformation: Example

$r_i(X); r_i(Y)$ $r_i(X); r_i(Y)$ $w_i(X); w_j(Y)$
--

$r_1(A); w_1(A); r_2(A); w_2(A); r_1(B); w_1(B); r_2(B); w_2(B)$

$r_1(A); w_1(A); r_2(A); r_1(B); w_2(A); w_1(B); r_2(B); w_2(B)$

$r_1(A); w_1(A); r_1(B); r_2(A); w_2(A); w_1(B); r_2(B); w_2(B)$

$r_1(A); w_1(A); r_1(B); r_2(A); w_1(B); w_2(A); r_2(B); w_2(B)$

$r_1(A); w_1(A); r_1(B); w_1(B); r_2(A); w_2(A); r_2(B); w_2(B)$



Enforcing Serializability

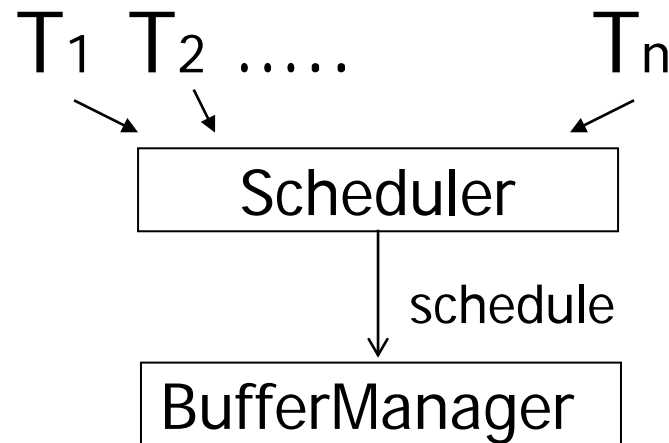


How to enforce serializable schedules?

Option 1: run system, recording $P(S)$; at end of day, check for $P(S)$ cycles and declare if execution was good! **Unrealistic...!**

How to enforce serializable schedules?

Option 2: prevent P(S) cycles from occurring



But how ???

2.A) Buffer transactions during n seconds, stop DBMS, make schedule, execute schedule, repeat...

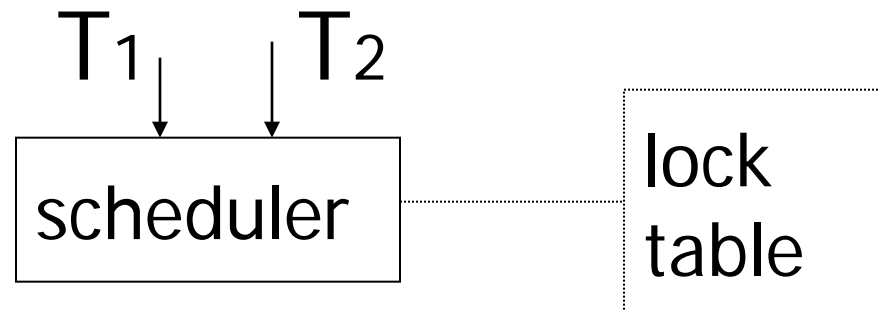
unrealistic...!

2.B) Use a locking protocol!

Two new actions:

lock (exclusive): $l_i(A)$

unlock: $u_i(A)$





Rule #1: Well-formed transactions

$T_i: \dots l_i(A) \dots p_i(A) \dots u_i(A) \dots$



Exercise:

- What schedules are legal?

What transactions are well-formed?

$S1 = I_1(A)I_1(B)r_1(A)w_1(B)I_2(B)u_1(A)u_1(B)$

$r_2(B)w_2(B)u_2(B)I_3(B)r_3(B)u_3(B)$



Exercise:

- What schedules are legal?

What transactions are well-formed?

$S1 = I_1(A)I_1(B)r_1(A)w_1(B)I_2(B)u_1(A)u_1(B)$

$r_2(B)w_2(B)u_2(B)I_3(B)r_3(B)u_3(B)$



Exercise:

- What schedules are legal?

What transactions are well-formed?

$S1 = I_1(A)I_1(B)r_1(A)w_1(B)I_2(B)u_1(A)u_1(B)$

$r_2(B)w_2(B)u_2(B)I_3(B)r_3(B)u_3(B)$

$S2 = I_1(A)r_1(A)w_1(B)u_1(A)u_1(B)$

$I_2(B)r_2(B)w_2(B)I_3(B)r_3(B)u_3(B)$

Exercise:

- What schedules are legal?

What transactions are well-formed?

$S1 = I_1(A)I_1(B)r_1(A)w_1(B)I_2(B)u_1(A)u_1(B)$

$r_2(B)w_2(B)u_2(B)I_3(B)r_3(B)u_3(B)$

$S2 = I_1(A)r_1(A)w_1(B)u_1(A)u_1(B)$

$I_2(B)r_2(B)w_2(B)I_3(B)r_3(B)u_3(B)$

Exercise:

- What schedules are legal?

What transactions are well-formed?

S1 = $l_1(A)l_1(B)r_1(A)w_1(B)l_2(B)u_1(A)u_1(B)$
 $r_2(B)w_2(B)u_2(B)l_3(B)r_3(B)u_3(B)$

S2 = $l_1(A)r_1(A)w_1(B)u_1(A)u_1(B)$
 $l_2(B)r_2(B)w_2(B)l_3(B)r_3(B)u_3(B)$

S3 = $l_1(A)r_1(A)u_1(A)l_1(B)w_1(B)u_1(B)$
 $l_2(B)r_2(B)w_2(B)u_2(B)l_3(B)r_3(B)u_3(B)$

Exercise:

- What schedules are legal?

What transactions are well-formed?

S1 = $l_1(A)l_1(B)r_1(A)w_1(B)l_2(B)u_1(A)u_1(B)$
 $r_2(B)w_2(B)u_2(B)l_3(B)r_3(B)u_3(B)$

S2 = $l_1(A)r_1(A)w_1(B)u_1(A)u_1(B)$
 $l_2(B)r_2(B)w_2(B)l_3(B)r_3(B)u_3(B)$

S3 = $l_1(A)r_1(A)u_1(A)l_1(B)w_1(B)u_1(B)$
 $l_2(B)r_2(B)w_2(B)u_2(B)l_3(B)r_3(B)u_3(B)$



Locking Example

T1: Read(A); A =A+100; Write(A);
 Read(B); B=B+100; Write(B);

T2: Read(A); A =A*2; Write(A);
 Read(B); B=B*2; Write(B);



Serial Schedule

T1	T2
Read(A)	
$A \leftarrow A + 100$; Write(A)	
Read(B);	
$B \leftarrow B + 100$; Write(B);	
	Read(A)
	$A \leftarrow Ax2$; Write(A);
	Read(B)
	$B \leftarrow Bx2$; Write(B);

A	B
25	25
125	
	125
250	
	250
250	250

Schedule A

T1

 $l_1(A); \text{Read}(A)$ $A \leftarrow A + 100; \text{Write}(A); u_1(A)$ $l_1(B); \text{Read}(B)$ $B \leftarrow B + 100; \text{Write}(B); u_1(B)$

T2

 $l_2(A); \text{Read}(A)$ $A \leftarrow Ax2; \text{Write}(A); u_2(A)$ $l_2(B); \text{Read}(B)$ $B \leftarrow Bx2; \text{Write}(B); u_2(B)$

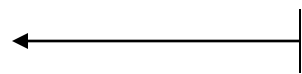


Schedule A

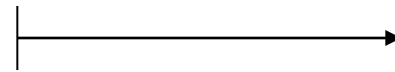
		A	B
T1	T2	25	25
$I_1(A); \text{Read}(A)$			
$A \leftarrow A + 100; \text{Write}(A); u_1(A)$		125	
	$I_2(A); \text{Read}(A)$		
	$A \leftarrow Ax2; \text{Write}(A); u_2(A)$	250	
	$I_2(B); \text{Read}(B)$		
	$B \leftarrow Bx2; \text{Write}(B); u_2(B)$		50
$I_1(B); \text{Read}(B)$			
$B \leftarrow B + 100; \text{Write}(B); u_1(B)$			150
		250	150

Rule #3 Two phase locking (2PL) for transactions

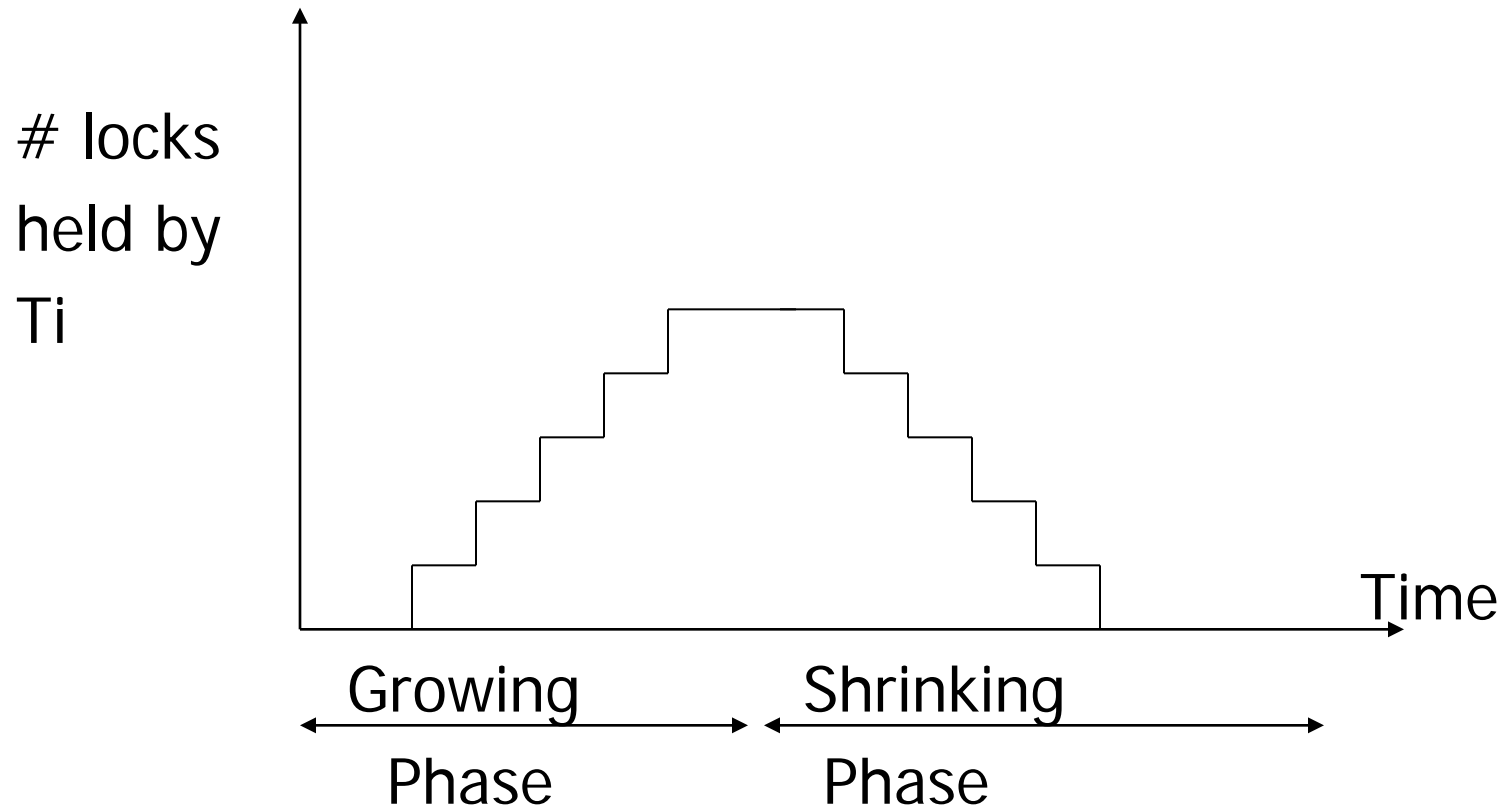
$T_i = \dots \text{li}(A) \dots \text{ui}(A) \dots$



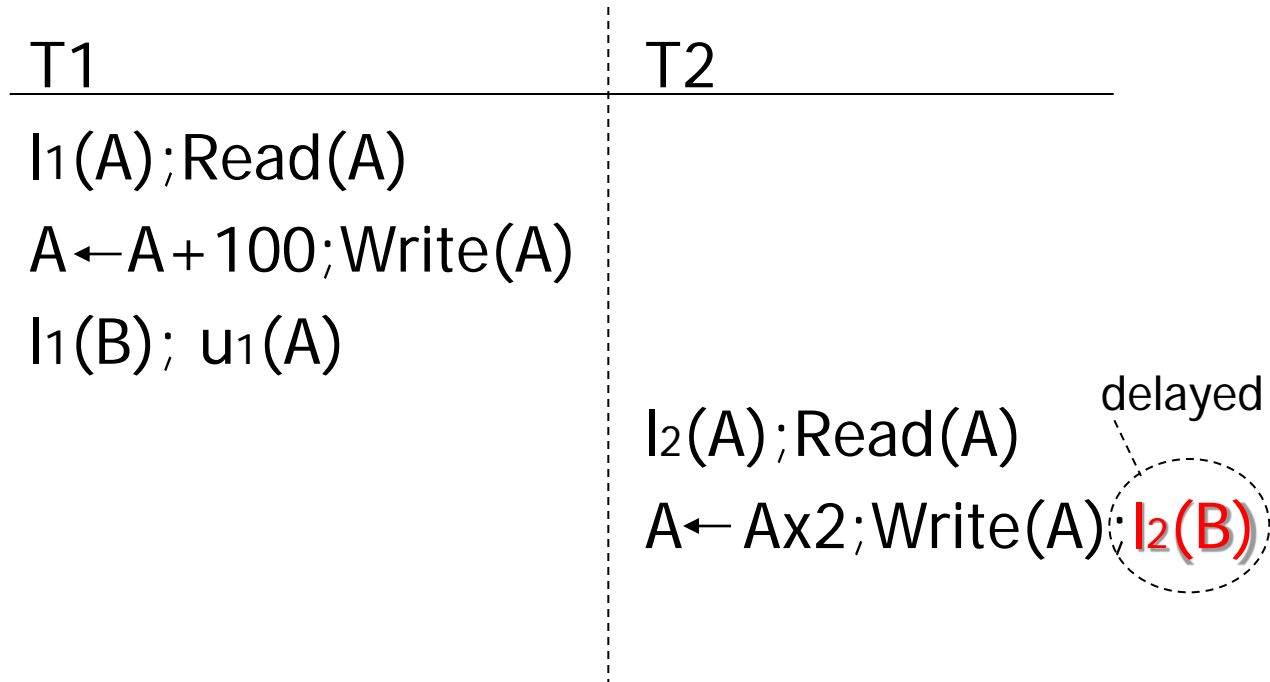
no unlocks



no locks



Schedule B



Schedule B

T1

I₁(A); Read(A)

A ← A + 100; Write(A)

I₁(B); u₁(A)

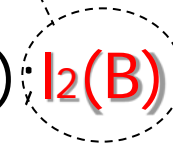
Read(B); B ← B + 100

Write(B); u₁(B)

T2

I₂(A); Read(A)A ← Ax2; Write(A); I₂(B)

delayed





Schedule B

T1	T2
$I_1(A); \text{Read}(A)$	
$A \leftarrow A + 100; \text{Write}(A)$	
$I_1(B); u_1(A)$	
	$I_2(A); \text{Read}(A)$ delayed
	$A \leftarrow A \times 2; \text{Write}(A); I_2(B)$
$\text{Read}(B); B \leftarrow B + 100$	
$\text{Write}(B); u_1(B)$	
	$I_2(B); u_2(A); \text{Read}(B)$
	$B \leftarrow B \times 2; \text{Write}(B); u_2(B);$

A	B
25	25
125	
250	
	125
	250
250	250